## Mathematics

 At Ashmole Drimary

Mental Calculation Dolicy

## National Curriculum Sep 2014

## Statutory/non statutory guidance

## Mental calculation skills derived from guidance (from National strategy Teaching children to calculate mentally)

## Numbers and the number system

Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number
Count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens
Given a number, identify one more and one less

## Addition and subtraction

Pupils memorise and reason with number bonds to 10 and 20 in several forms (for example, $9+7=9+7=16 ; 16-7=$ 9; 7 = $16-9$ )

Recall number pairs with a total of 10 and 20 , e.g. $3+7$, or what to add to a single-digit number to make 10 and 20, e.g. $3+$ T= 10
Recall addition and subtraction facts for all numbers to 20 , e.g. $9+8,17-9$, drawing on knowledge of inverse operations
Add or subtract a pair of single-digit numbers, e.g. $4+5,8-3$
Add or subtract a single-digit number to or from a teens number, e.g. $13+5,17-3$
Add or subtract a single-digit to or from 10, and add a multiple of 10 to a single-digit number, e.g. $10+7,7+30$

Add near doubles, e.g. $6+7$ addition and subtraction facts for all numbers up to at least 20, e.g. $9+7=9+7=16 ; 16-7=9 ; 7=16-9$
Add or subtract a pair of single-digit numbers, including crossing 10, e.g. $5+8,12-7$
Add any single-digit number to or from a multiple of 10 , e.g. $60+5$
Subtract any single-digit number from a multiple of 10, e.g. 80-7
Add or subtract a single digit number to or from a two-digit number, including crossing the tens boundary, e.g. $23+5,57-3$, then $28+5,52-7$
Add or subtract a multiple of 10 to or from any two-digit number, e.g. $27+60,72-50$ Add 9, $19,29, \ldots$ or $11,21,31, \ldots$
Add near doubles, e.g. $13+14,39+40$
Recall doubles of all numbers to 10, e.g. double 6
Recall doubles of all numbers to 10 and corresponding halves to 20
Recall odd and even numbers to 20
Count on from and back to zero in ones, twos, fives or tens

| Year 2 | Numbers and the number system <br> Count in steps of 2,3 , and 5 from 0 , and in tens from any number, forward and backward <br> Recognise the place value of each digit in a two-digit number (tens, ones) <br> Identify, represent and estimate numbers using different representations, including the number line <br> Compare and order numbers from 0 up to 100 ; use $<,>$ and $=$ signs read and write numbers to at least 100 in numerals and in words |  |
| :---: | :---: | :---: |
|  | Addition and subtraction <br> Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 <br> Add and subtract numbers mentally, including: <br> a two-digit number and ones <br> a two-digit number and tens <br> two two-digit numbers <br> Adding three one-digit numbers <br> Show that addition of two numbers can be done in any order(commutative) and subtraction of one number from another cannot <br> Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. | Recall all pairs of multiples of 10 with totals up to 100 , e.g. $30+70$, or $60+$ T $=100$ <br> Recall what must be added to any two-digit number to make the next multiple of 10, e.g. $52+$圂= 60 <br> Recall addition doubles for all numbers to 20 , e.g. $17+17$ and multiples of 10 to 50 , e.g. $40+40$ <br> Count in fractions up to 10 , starting from any number using the $1 / 2$ and $2 / 4$ equivalence on the number line ( $11 / 2,12 / 4$ ) <br> Add and subtract groups of small numbers, e.g. 5-3+2 <br> Add or subtract a two-digit number to or from a multiple of 10, e.g. $50+38,90-27$ <br> Add and subtract two-digit numbers e.g. $34+65,68-35$ <br> Add near doubles, e.g. $18+16,60+70$ <br> Recall sums and differences of multiples of 10, e.g. $50+80,120-90$ <br> Recall pairs of two-digit numbers with a total of 100, e.g. $32+68$, or $32+$ ? $=100$ <br> Recall addition doubles for multiples of 10 to 100, e.g. $90+90$ |
|  | Multiplication and division <br> Recall multiplication facts for the 2, 5 and 10 times-tables, and corresponding division facts <br> Solve problems involving multiplication and division using mental methods | Recall doubles of all numbers to 20 e.g. double 13, and corresponding halves <br> Recall doubles of multiples of 10 to 50, e.g. double 40, and corresponding halves <br> Recall odd and even numbers to 100 <br> Recall doubles of numbers 1 to 100, e.g. double 58, corresponding halves <br> Recall double any multiple of 5 up to 100, e.g. double 35 <br> Halve any multiple of 10 up to 200 , e.g. halve 170 <br> Find unit fractions of numbers and quantities involving halves, thirds, quarters, fifths and tenths |


| Year 3 | Numbers and the number system <br> Count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 Recognise the place value of each digit in a three-digit numb Compare and order numbers up to 1000 Identify, represent and estimate numbers using different rep Read and write numbers up to 1000 in numerals and in words | more or less than a given number (hundreds, tens, ones) <br> resentations |
| :---: | :---: | :---: |
|  | Addition and subtraction <br> Add and subtract numbers mentally, including: <br> a three-digit number and ones <br> a three-digit number and tens <br> a three-digit number and hundreds <br> For mental calculations with two-digit numbers, the answer could exceed 100 | Recall sums and differences of pairs of multiples of 10,100 or 1000 e.g. $50+80,120-90$ Recall addition doubles of numbers 1 to 100 , e.g. $38+38$, and the corresponding halves Add or subtract any pair of two-digit numbers, including crossing the tens and 100 boundary, e.g. $47+58,91-35,32+$ 回 $=100$ <br> Add or subtract a near multiple of 10, e.g. $56+29,86-38$ <br> Add near doubles of two-digit numbers, e.g. $38+37$ <br> Add or subtract two-digit or three-digit multiples of 10, e.g. $120-40,140+150,370-180$ <br> Recall addition doubles for multiples of 10 to 100, e.g. $90+90$ |
|  | Multiplication and division <br> Recall multiplication facts for the 3,4 , and 8 times-tables, and corresponding division facts Recall multiplication tables including two-digit numbers times one-digit numbers, using mental methods <br> Count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 compare and order unit fractions, and fractions with the same denominators | Recall doubles of numbers 1 to 100, e.g. double 58, and corresponding halves <br> Multiply one-digit or two-digit numbers by 10 or 100 , e.g. $7 \times 100,46 \times 10,54 \times 100$ <br> Double any two-digit number, e.g. double 39 <br> Double any multiple of 10 or 100, e.g. double 340 , double 800 , and halve the corresponding multiples of 10 and 100 <br> Halve any even number to 200 <br> Find unit fractions and simple non-unit fractions of numbers and quantities, e.g. 3/8 of 24 Multiply and divide two-digit numbers by 4 or 8 , e.g. $26 \times 4,96 \div 8$ |


| Year 4 | Numbers and the number system <br> Count in multiples of $6,7,9,25$ and 1000 <br> Find 1000 more or less than a given number <br> Count backwards through zero to include negative numbers <br> Recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) <br> Order and compare numbers beyond 1000 <br> Identify, represent and estimate numbers using different representations <br> Round any number to the nearest 10,100 or 1000 <br> Round decimals with one decimal place to the nearest whole number |  |
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|  | Addition and subtraction <br> Pupils continue to practise mental methods with increasingly large numbers to aid fluency to at least 1000 Count backwards through zero to include negative numbers <br> Count up and down in hundredths; recognise that hundredths arise when dividing an object by 100 and dividing tenths by ten. | Add or subtract a pair of two-digit numbers or three-digit multiples of 10, e.g. $38+86,620-$ $380,350+360$ <br> Add or subtract a near multiple of 10 or 100 to any two-digit or three-digit number, e.g. $235+$ 198 <br> Find the difference between near multiples of 100, e.g. $607-588$, or of 1000, e.g. 6070-4087 sums and differences of decimals, e.g. $6.5+2.7,7.8-1.3$ <br> Doubles and halves of decimals, e.g. half of 5.6 , double 3.4 <br> what must be added to any four-digit number to make the next multiple of 1000, e.g. $4087+$ ? $=5000$ <br> What must be added to a decimal with units and tenths to make the next whole number, e.g. $7.2+\text { 回 }=8$ |
|  | Multiplication and division <br> Multiplication facts to $12 \times 12$ and the corresponding division facts <br> Count in multiples of 6, 7, 9, 25 and 1000 <br> Use place value, known and derived facts to multiply and Divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers <br> Recognise and write decimal equivalents of any number of tenths or hundredths <br> Recognise and write decimal equivalents to $1 / 4,1 / 2,3 / 4$ | Squares to $10 \times 10$ <br> Division facts corresponding to tables up to $10 \times 10$, and the related unit fractions, e.g. $7 \times 9=$ <br> 63 so one-ninth of 63 is 7 and one-seventh of 63 is 9 <br> Percentage equivalents of one-half, one-quarter, three-quarters, tenths and hundredths <br> factor pairs to 100 <br> Multiply and divide numbers to 1000 by 10 and then 100 (whole-number answers), e.g. $325 \times 10$, $42 \times 100,120 \div 10,600 \div 100,850 \div 10$ <br> Multiply a multiple of 10 to 100 by a single-digit number, e.g. $40 \times 3$ <br> Multiply numbers to 20 by a single-digit, e.g. $17 \times 3$ <br> Identify the remainder when dividing by 2,5 or 10 <br> Give the factor pair associated with a multiplication fact, e.g. identify that if $2 \times 3=6$ then 6 has the factor pair 2 and 3 multiply two-digit numbers by 5 or 20 , e.g. $320 \times 5,14 \times 20$ |


|  | Pupils continue to practise recalling and using multiplication tables and related division facts to aid fluency. <br> Pupils practise mental methods and extend this to threedigit numbers to derive facts, (for example $600 \div 3=200$ can be derived from $2 \times 3=6$ ). <br> Recognise and use factor pairs and commutativity in mental calculations | Multiply by 25 or 50, e.g. $48 \times 25,32 \times 50$ <br> Double three-digit multiples of 10 to 500, e.g. $380 \times 2$, and find the corresponding halves, e.g. $760 \div 2$ <br> Find the remainder after dividing a two-digit number by a single-digit number, e.g. $27 \div 4=6 R$ <br> 3 <br> Multiply and divide whole numbers and decimals by 10,100 or 1000 , e.g. $4.3 \times 10,0.75 \times 100,25$ $\div 10,673 \div 100,74 \div 100$ <br> Multiply pairs of multiples of 10 , e.g. $60 \times 30$, and a multiple of 100 by a single digit number, e.g. $900 \times 8$ <br> Divide a multiple of 10 by a single-digit number (whole number answers) e.g. $80 \div 4,270 \div 3$ <br> Find fractions of whole numbers or quantities, e.g. 2 <br> 3 of 27,45 of 70 kg <br> Find $50 \%, 25 \%$ or $10 \%$ of whole numbers or quantities, e.g. $25 \%$ of $20 \mathrm{~kg}, 10 \%$ of $£ 80$ <br> Find factor pairs for numbers to 100, e.g. 30 has the factor pairs $1 \times 30,2 \times 15,3 \times 10$ and $5 \times 6$ |
| :---: | :---: | :---: |
| Year 5 | Numbers and the number system <br> Read, write, order and compare numbers to at least 1000000 and determine the value of each digit <br> Count forwards or backwards in steps of powers of 10 for any given number up to 1000000 <br> Interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero Round any number up to 1000000 to the nearest 10, 100, 1000, 10000 and 100000 |  |
|  | Addition and subtraction <br> Add and subtract numbers mentally with increasingly large numbers with more than 4 digits <br> They practise mental calculations with increasingly large numbers to aid fluency (for example, $12462-2300=10$ 162). <br> They mentally add and subtract tenths, and one-digit whole numbers and tenths. <br> They practise adding and subtracting decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 (for example, $0.83+0.17=1$ ). | What must be added to any four-digit number to make the next multiple of 1000, e.g. $4087+$国= 5000 <br> Addition and subtraction facts for multiples of 10 to 1000 and decimal numbers with one decimal place, e.g. $650+$ ? $=930$, ${ }^{2}-1.4=2.5$ <br> What must be added to a decimal with units, tenths and hundredths to make the next whole number, e.g. $7.26+$ 囵 $=8$ <br> Add or subtract pairs of decimals with units, tenths or hundredths, e.g. $0.7+3.38$ <br> Find doubles of decimals each with units and tenths, e.g. 1.6 + 1.6 <br> Add near doubles of decimals, e.g. $2.5+2.6$ <br> Add or subtract a decimal with units and tenths, that is nearly a whole number, e.g. 4.3 + 2.9, $6.5-3.8$ |

## Multiplication and division

Multiply and divide numbers mentally drawing upon known facts of multiplication to $12 \times 12$ table

They apply all the multiplication tables and related division facts frequently
Pupils use multiplication and division as inverse
Squares, cubes and primes of the corresponding multiples of 12

Percentage equivalents of one-half, one-quarter, threequarters, tenths and hundredths

Squares, cubes and primes to $12 \times 12$
Squares of the corresponding multiples of 10
Prime numbers less than 100
Equivalent fractions, decimals and percentages for hundredths, e.g. $35 \%$ is equivalent to 0.35 or 35/100
Division facts corresponding to tables up to $10 \times 10$, and the related unit fractions, e.g. $7 \times 9=$ 63 so one-ninth of 63 is 7 and one-seventh of 63 is 9
Multiply pairs of two-digit and single-digit numbers, e.g. $28 \times 3$
Divide a two-digit number by a single-digit number, e.g. $68 \div 4$
Divide by 25 or 50 , e.g. $480 \div 25,3200 \div 50$
Double decimals with units and tenths, e.g. double 7.6, and find the corresponding halves, e.g. half of 15.2
Multiply pairs of multiples of 10 and 100, e.g. $50 \times 30,600 \times 20$
Divide multiples of 100 by a multiple of 10 or 100 (whole number answers), e.g. $600 \div 20,800 \div$ $400,2100 \div 300$
Multiply and divide two-digit decimals such as $0.8 \times 7,4.8 \div 6$
Find $10 \%$ or multiples of $10 \%$, of whole numbers and quantities, e.g. $30 \%$ of $50 \mathrm{ml}, 40 \%$ of $£ 30$, $70 \%$ of 200 g
Simplify fractions by cancelling
Scale up and down using known facts, e.g. given that three oranges cost 24 p, find the cost of four oranges
Identify numbers with odd and even numbers of factors and no factor pairs other than 1 and themselves

| 6 | Numbers and the number system <br> Read, write, order and compare numbers up to 10000000 and determine the value of each digit Round any whole number to a required degree of accuracy <br> Use negative numbers in context, and calculate intervals across zero |  |
| :---: | :---: | :---: |
|  | Addition and subtraction Multiplication and division <br> Perform mental calculations including mixed operations and large numbers <br> Pupils continue to use all the multiplication tables to calculate mathematical statements in order to maintain their fluency. <br> Recall and use equivalences between simple fractions, decimals and percentages, including in different contexts <br> Pupils can explore and make conjectures about converting a simple fraction to a decimal fraction (for example, $3 \div 8=$ 0.375). <br> Pupils multiply decimals by whole numbers, starting with the simplest cases, such as $0.4 \times 2=0.8$, and in practical contexts, such as measures and money. <br> They recognise division calculations as the inverse of multiplication. | Use the commutative, associative and distribute laws. <br> -Commutative law e.g. $4 \times 7 \times 5=4 \times 5 \times 7=20 \times 7=140$ <br> -Associative law e.g. $15 \times 33=(5 \times 3) \times 33$ or $5 \times(3 \times 33)=5 \times 99=495$ <br> -Distributive law e.g. $3.7 \times 99=3.7 \times(100-1)$ $\begin{aligned} & =(3.7 \times 100)-(3.7 \times 1) \\ & =370-3.7 \quad=366.3 \end{aligned}$ <br> A quotient (the result obtained after division) can be expressed as a fraction or as a decimal, e.g. $90 \div 13=6^{12} / 13 \quad 90 \div 13=6.92$ (rounded to two decimal places). <br> Understand that multiplication and division are inverse operations, and use this to check result, e.g. $6783 \div 19=357$ appears to be about right because $350 \times 20=7000$. <br> Relate division to fractions. Understand that: $1 / 4$ of 3.6 is equivalent to $3.6 \div 4 ; 7 \div 8$ is equivalent to $7 / 8 ; 50 / 3$ is equivalent to $50 \div 3$. <br> Know that the order of operations is: bracket, powers or indices, multiplication (including 'of') and division, addition and subtraction. <br> Calculate with mixed operations, including with a calculator. E.g. $32+13 \times 5=97$; $(32+13) \times 5$ $=225 ;\left(3^{2}+4^{2}\right)^{2}=625 ;\left(5^{2}-7\right) /\left(2^{2}-1\right)=6$ <br> Know with rapid recall addition and subtraction facts to 20. <br> Derive quickly doubles of two-digit numbers including decimals, e.g. $23 \times 2,3.8 \times 2,0.76 \times 2$ <br> Doubles of multiples of 10 to 1000 , e.g. $670 \times 2,830 \times 2$ <br> Doubles of multiples of 100 to 10000 , e.g. $1700 \times 2,6500 \times 2$ <br> And all the corresponding halves <br> Derive quickly whole-number complements in 100, e.g. $100=63+37$ <br> Decimal complements in 1 (one or two decimal places), e.g. $1=0.8+0.2,1=0.41+0.59$ <br> Recall rapidly or derive quickly simple decimal/fraction/percentage equivalents, such as: $1 / 8=0.125 \text { or } 121 / 2 \%, \quad 0.23 \text { is equivalent to } 23 \% \text {, }$ <br> $13 / 4=1.75$ or $175 \%$, $57 \%$ is equivalent to 0.57 or $57 / 100$ <br> Simple addition facts for fractions, such as $1 / 4+1 / 4=1 / 2 ; 1 / 4+1 / 2=3 / 4$ |



Count forwards and backwards from any number. E.g. Count on in 0.1s from 4.5; Count back from 4.05 in 0.01 s; Count on from and back to zero in steps of $3 / 4$ Add mentally several small positive or negative numbers. E.g. $4+8+12+6+13 ; 5+(-4)+8+(-$ 10) $+(-7)$

Extend to calculating a mean using an assumed mean. E.g. Find the mean of 18.7, 18.4, 19.1, 18.3 and 19.5. Use 19.0 as the assumed mean. The differences are $-0.3,-0.6,0.1,-0.7$ and 0.5 , giving a total difference of -1.0 . The actual mean is $19.0-(1.0 \div 5)=18.8$.
Continue to add and subtract any pair of two-digit whole numbers, such as $76+58,91-47$ Extend to adding and subtracting a two-digit whole number to or from a three-digit whole number; adding and subtracting decimals, e.g. $8.6 \pm 5.7,0.76 \pm 0.58$.
Use near doubles. E.g $8.5+8.2=16.7$ (double 8.2 plus 0.3 ); $427+366=793$ (double 400 plus 27 minus 34).
Use the relationship between addition and subtraction. E.g. recognise that knowing one of: $2.4+5.8=8.2 ; 5.8+2.4=8.2 ; 8.2-5.8=2.4 ; 8.2-2.4=5.8$, means that you also know the other three.
Use factors. E.g. $4.5 \times 1.8 \quad 4.5 \times 6=27 \quad 27 \times 3=81$
$3.2 \times 30 \quad 3.2 \times 10=32 \quad 32 \times 3=96$
$\begin{array}{lll}220.02 & 22 \times 0.01=0.22 & 0.22 \times 2=0.44 \\ 420 \div 15 & 420 \div 5=84 & 84 \div 3=28\end{array}$
Use known facts such as $1 / 5=0.2$ to calculate mentally $3 / 5=3 \times 0.2=0.6$.
Convert between improper fractions and mixed numbers. E.g. Convert $7 \frac{1}{3}$ into an improper fraction; Convert $36 / 5$ into a mixed number.
Find simple equivalent fractions. E.g. State three fractions equivalent to $3 / 5$, such as: $6 / 10,30 / 50$, 24/40

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\text { Fill in the boxes: } 3 / 4=/ 8=/ 12=\quad / 16=\quad / 20 ; \quad 7 /=21 / 30
$$

Convert between fractions, decimals and percentages. E.g. Convert 23\% into a decimal (Know that $23 \%$ is equivalent to $23 / 100$ or 0.23 .); Convert $3 / 5$ into a percentage (Know that $3 / 5=6 / 10$ or ${ }^{60} / 100$, so it is equivalent to $60 \%$.); Express $55 \%$ as a fraction in its lowest terms (Know that $55 \%$ is equivalent to $55 / 100$, and cancel this to $11 / 20$.)

